

A competitive complex formation mechanism underlies trichome patterning on *Arabidopsis* leaves

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Trichome patterning in *Arabidopsis* serves as a model system for *de novo* pattern formation in plants. It is thought to typify the theoretical activator–inhibitor mechanism, although this hypothesis has never been challenged by a combined experimental and theoretical approach. By integrating the key genetic and molecular data of the trichome patterning system, we developed a new theoretical model that allows the direct testing of the effect of experimental interventions and in the prediction of patterning phenotypes. We show experimentally that the trichome inhibitor *TRIPTYCHON* is transcriptionally activated by the known positive regulators *GLABRA1* and *GLABRA3*. Further, we demonstrate by particle bombardment of protein fusions with GFP that *TRIPTYCHON* and *CAPRICE* but not *GLABRA1* and *GLABRA3* can move between cells. Finally, theoretical considerations suggest promoter swapping and basal overexpression experiments by means of which we are able to discriminate three biologically meaningful variants of the trichome patterning model. Our study demonstrates that the mutual interplay between theory and experiment can reveal a new level of understanding of how biochemical mechanisms can drive biological patterning processes.

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Introduction

Most theoretical models in biology aiming to explain *de novo* creation of regular spacing patterns are based on either of two principles: activator–inhibitor or substrate depletion (Gierer and Meinhardt, 1972). In both cases, pattern formation relies on a dynamic instability first suggested by Turing (1952) in the context of morphogenesis. The initiation of *Arabidopsis* trichomes on the leaf blade serves as an excellent model system to study the molecular mechanism underlying *de novo* patterning. Trichomes are leaf hairs derived from epidermal cells that are formed in a regular spacing pattern in a rapidly growing cell layer at the leaf base. New trichomes are formed at a minimal distance of three or four cells from already existing ones and their position is not correlated with any other recognizable positional landmark (Hulskamp *et al.*, 1994). A mechanism by which the spacing pattern is achieved by a conserved cell division pattern was excluded by clonal

analysis (Larkin *et al.*, 1996; Schnittger *et al.*, 1999). Thus, all data indicate that a *de novo* patterning mechanism is operating. Several independent mutational screens have identified genes that appear to act as positive or negative regulators of trichome initiation. The corresponding mutants of the positive regulators have fewer or no trichomes. They include the R2R3 MYB transcription factors *GLABRA1* (*GL1*) and MYB23 (Oppenheimer *et al.*, 1991; Kirik *et al.*, 2001, 2005), the bHLH factors *GLABRA3* (*GL3*) and *ENHANCER OF GLABRA3* (*EGL3*) (Payne *et al.*, 2000; Zhang *et al.*, 2003; Bernhardt *et al.*, 2005) and the WD40-repeat protein *TRANSPARENT TESTA GLABRA1* (*TTG1*) (Galway *et al.*, 1994; Walker *et al.*, 1999a). Yeast two-hybrid data suggest the formation of a trichome-promoting trimeric complex, due to binding of one R2R3 MYB factor and *TTG1* to a bHLH factor (Payne *et al.*, 2000). The negative regulators *TRIPTYCHON* (*TRY*) and *CAPRICE* (*CPC*) were initially identified by mutants showing

trichome clusters (Schellmann *et al*, 2002) and a higher trichome density (Wada *et al*, 1997a), respectively. Both genes encode homologous single-repeat MYB-related transcription factors (Wada *et al*, 1997a; Schellmann *et al*, 2002). Later, four further homologues were found that act in a partially redundant manner, namely *ENHANCER OF TRY AND CPC1* (*ETC1*) (Kirik *et al*, 2004a), *ETC2* (Kirik *et al*, 2004b), *TRICHOMELESS1* (Wang *et al*, 2007) and *CAPRICE-LIKE MYB3* (*CPL3*) (Tominaga *et al*, 2008). These inhibitors can compete with the R2R3 MYB factor for binding to GL3/EGL3 in yeast three-hybrid assays (Esch *et al*, 2003). Therefore, current models assume that these inhibitors counteract the trimeric active complex by this competition mechanism under the assumption that the single-repeat MYB factor-containing complex is inactive (Larkin *et al*, 1996; Scheres, 2002; Marks and Esch, 2003; Pesch and Hulskamp, 2004; Ishida *et al*, 2008). It is assumed that the generation of the actual spacing pattern is mediated by the movement of the inhibitors. One downstream target of this machinery is the homeobox transcription factor *GLABRA2* (*GL2*), which is thought to trigger the actual process of trichome formation (Rerie *et al*, 1994; Cristina *et al*, 1996).

Virtually the same gene cassette is operating during epidermal root hair determination. Root hairs are arranged in cell files and only epidermal cells overlying a cleft between two cortex cells develop into root hairs (Dolan *et al*, 1994; Berger *et al*, 1998). Although this suggests that cell fate is determined by position; root hair fate depends largely on the R2R3 MYB factor WEREWOLF, TTG1, GL3/EGL3 and the inhibitors CPC, TRY and ETC1. Taken together, these genes activate the expression of *GL2* in non-root hair cells, where *GL2* represses root hair development (Larkin *et al*, 1996; Scheres, 2002; Marks and Esch, 2003; Pesch and Hulskamp, 2004; Ishida *et al*, 2008). Thus, in contrast to trichome development on leaves, the default fate in the root epidermis is the formation of root hairs.

In this study, we create a theoretical model based on the current knowledge of the trichome patterning system. We verify experimentally the previous assumption that the expression of the inhibitor *TRY* is induced by the positive regulators. Further, we find (Payne *et al*, 2000; Zhang *et al*, 2003) that the inhibitors *TRY* and *CPC* are mobile, whereas *GL1* and *GL3* are cell autonomous. Protein interaction assays suggest three alternative scenarios by which the positive regulators are inhibited. A combination of overexpression experiments and theoretical modelling allows in the identification of the most relevant inhibition scenario for trichome patterning.

Results

Mathematical modelling and simulation of trichome patterning

We develop our initial model from the following assumptions, most of which are based on already published data in the context of trichome or root hair patterning: (1) the *GL1* *GL3* complex is considered to be the transcriptionally active complex (Morohashi *et al*, 2007); (2) similar to *GL3* and *WEREWOLF* in the root hair system, it is assumed that *GL1*

GL3 activate *TRY* (Bernhardt *et al*, 2005); (3) *TRY* counteracts the *GL1* *GL3* activity by competing with *GL1* for binding to *GL3* (Esch *et al*, 2003); (4) similar to that shown for *CPC* in the root, it is assumed that *TRY* protein can move between cells (Kurata *et al*, 2005). Further, we consider *GL3* to be mobile because *GL3* can travel between cells in the root (Bernhardt *et al*, 2005) and *GL1* to be immobile (Hulskamp *et al*, 1994); (5) as observed for the *GL3* homologue *TT8* and the *GL1* homologue *TT2*, it is assumed that the active complex, *GL1* *GL3*, activates the expression of *GL3* (Baudry *et al*, 2006); (6) *TTG1* is not taken into account as it is not essential for trichome formation as indicated by the fact that *GL1* and *GL3* overexpression or *GL1* overexpression in *try* mutants rescues the *ttg1* phenotype (Schnittger *et al*, 1998); (7) *GL2* is considered as a downstream target gene of this machinery (Rerie *et al*, 1994; Cristina *et al*, 1996); (8) *GL1* and *GL3* are expressed ubiquitously in the patterning zone (Larkin *et al*, 1993; Zhang *et al*, 2003); (9) in addition, it is assumed that *GL1* is activated by the active complex. This is included as a prerequisite for the model; (10) it is further assumed that all proteins are linearly degraded. The resulting interactions are shown in Figure 1 and the corresponding mathematical model is presented in the Materials and methods section.

Simulations of the corresponding differential equations reveal a regular spacing pattern for biologically reasonable parameter ranges. To further validate our model, we directly tested several of our key assumptions that have so far only been based on indirect genetic experiments or made by analogy to the root hair system.

***TRY* is transcriptionally activated by the active complex and suppresses its own transcription**

The transcriptional regulation of *TRY* was analysed using a *TRY:GUS* construct containing a promoter previously shown to truly reflect the endogenous expression (Schellmann *et al*, 2002). Trichome initiation takes place only at the base of young leaves (Figure 2, indicated by a red square). In this region, *TRY* is expressed in all epidermal cells. Expression in trichomes is stronger than in the surrounding epidermis (Schellmann *et al*, 2002). To corroborate the assumption that the active complex promotes the inhibitor, only those aspects of *TRY* expression are relevant that occur before or at the time of trichome initiation, i.e. the ubiquitous epidermal expression. This ubiquitous expression is absent in *gl1*, *gl3* and *gl3 egl3* mutants, indicating that *TRY* is transcriptionally induced by the active complex (Figure 2). According to our model, the inhibitors should repress the active complex and therefore indirectly themselves. This is confirmed in plants overexpressing *TRY* or *CPC*. No *TRY* expression is observed in a *35S:TRY* or *35S:CPC* background (data not shown).

Subcellular localization and ability for intercellular movement of *TRY*, *CPC*, *GL1* and *GL3*

In our model, we assume that *TRY* and *GL3* can move into neighbouring cells similar to that shown for *CPC* (Kurata *et al*, 2005) and *GL3* (Bernhardt *et al*, 2005) in the root hair system and that *GL1* acts cell autonomously (Hulskamp *et al*, 1994).

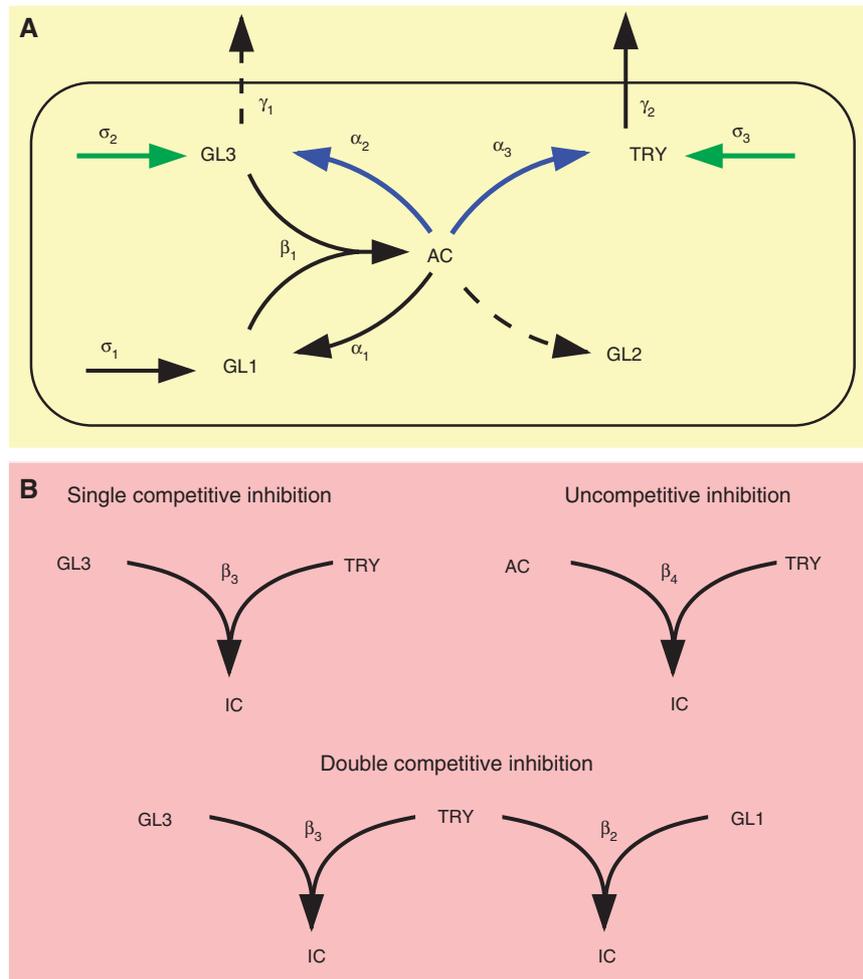


Figure 1 Mathematical modelling. **(A)** Activation part of the trichome patterning model. Solid lines indicate processes that are contained in the final model, whereas dashed lines indicate hypotheses that are rejected during the analysis. Greek letters denote the corresponding rate constants. The active complex (AC) induces the expression of the patterning genes *GLABRA1* (*GL1*), *GLABRA2* (*GL2*), *GLABRA3* (*GL3*) and *TRIPTYCHON* (*TRY*). *GL1* and *GL3* form the active complex by dimerization. *GL1*, *GL3* and *TRY* are basally expressed, and *GL3* and *TRY* are non-cell autonomous. Basal and AC-regulated expression (green and blue arrows) denote processes that are manipulated in the simulations and experiments. **(B)** Inhibition part of the trichome patterning model. The three inhibition scenarios characterize how *TRY* may inhibit the positive feedback described in (A). In the cases of single competitive inhibition, *TRY* prevents the formation of the active complex by binding to free *GL3*, whereas in the double competitive inhibition *TRY* binds additionally to free *GL1*. In case of uncompetitive inhibition, *TRY* directly binds to the existing active complex. In all scenarios, the resulting inactive complex is denoted by *IC*. The full model comprises the interactions shown in (A) and one of the inhibitions given in (B).

To test this in leaves, we fused the coding sequence of *TRY*, *CPC*, *GL1* and *GL3* to *GFP* and placed them under the control of the constitutive *CaMV 35S* promoter. *35S:GFP* and *35S:GFP:YFP* constructs served as controls and a *35S:YFP:peroxisome* marker was used to label the targeted cells. The functionality of the *TRY* and *CPC* fusion proteins was demonstrated by showing that their overexpression results in a loss of trichomes. The *GL1* and *GL3* fusion proteins have previously been shown to be functional by Esch *et al* (2003). *Arabidopsis* cotyledon and leaf epidermal cells were transformed by micro-projectile bombardment and analysed after 6–10 h. The *TRY* and *CPC* fusion proteins were localized in the targeted cell and in approximately one-third of the neighbouring cells. This demonstrates that these fusion proteins can move from the originally transformed cell to its neighbours (Figure 3; Tables I and II). *GFP-GL1* and surprisingly also

GFP-GL3 proteins did not move in this assay (Figure 3; Table I). The finding that *GL3* is cell autonomous is incorporated into our model.

TRY physically interacts with *GL1* and *GL3*

By assessing the interaction of *TRY* with other patterning genes using the bimolecular fluorescence complementation (BiFC) system and pull-down experiments, we confirmed the interaction between *TRY* and *GL3* and *EGL3* (Kirik *et al*, 2004b; Bernhardt *et al*, 2005) previously shown using yeast two-hybrid experiments (Figure 4). To our surprise, we also found an interaction of *TRY* with *GL1* in both assays. This suggests an additional inhibitory interaction where *TRY* competes with *GL3* for binding to *GL1*.

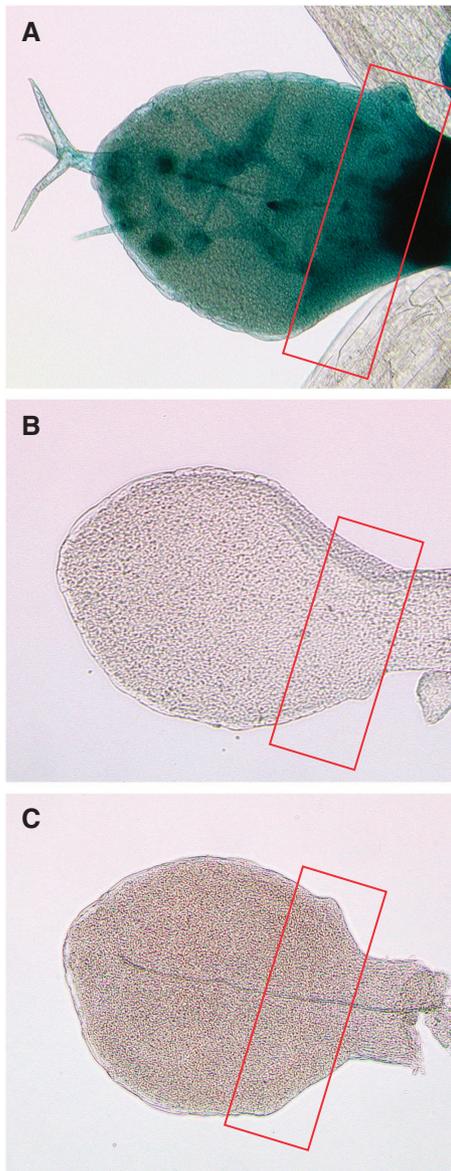


Figure 2 Expression of *TRY:GUS* in wild type and mutants. *TRY:GUS* expression is shown in young leaves: (A) wild type; (B) *gl3* and (C) *gl1-1*. Note that the ubiquitous expression at the leaf base is absent in all single mutants.

Challenging the system by overexpression experiments

The finding that GL1 can bind to TRY as well as the fact that TRY can bind to GL3 raises the possibility for three different inhibition scenarios (Figure 1B). (1) Single competitive inhibition: TRY binds to free GL3 and prevents GL1 GL3 dimerization; (2) Double competitive inhibition: TRY binds to free GL3 or GL1, thereby preventing the interaction between GL1 and GL3; (3) Uncompetitive inhibition: TRY binds to the GL1 GL3 dimer and represses its function. Although the double competitive model contains the single competitive model as an extreme case, the uncompetitive model is independent of the other two inhibition scenarios. In all three cases, we found

regular spacing patterns for biologically meaningful parameters, although with different parameter ranges and sensitivities (Supplementary Figure 4). This suggests manipulation of the system experimentally to discriminate the biological relevance of the three scenarios. We decided to consider overexpression of *TRY* and *GL3* either constitutively under the *35S* promoter or under the common downstream promoter of *GL2*. We created the respective plant lines to investigate the results of these experimental interventions. All *GL2:TRY* plants are completely glabrous in two independent lines. *35S:GL3* lines show a higher trichome density in the patterning zone (compare Figure 5B and C). In the most basal part of the leaf spanning the region containing only unbranched trichomes, a significant difference is found between wild-type Ler (9.2 ± 2.7 , $n=30$) and *35S:GL3* (14.7 ± 4.3 , $n=30$) by the Student's *t*-test ($P < 0.01$). However, in *GL2:GL3* lines, we observe no significant difference in trichome density in the patterning zone (wild type: 6.3 ± 1.7 , $n=30$; *GL2:GL3*: 7 ± 2.77 , $n=30$; compare Figure 5A and D). It is noteworthy that in both *GL3* overexpression lines, the mature part of the leaf displays additional young trichomes regularly scattered between fully mature trichomes. This situation is rarely found in wild-type Columbia ($7.3\% \pm 7.3$, $n=20$) and *Ler* ($7.8\% \pm 8.4$, $n=20$). In *GL2:GL3* and *35S:GL3*, they represent a significant fraction of all trichomes ($47\% \pm 7.3$, $n=21$) and ($44.1\% \pm 11.5$, $n=22$), respectively. This indicates that these young trichomes are formed later in leaf development, suggesting that the time window allowing trichome formation is expanded in *GL2:GL3* and *35S:GL3* lines.

We simulated the corresponding overexpression experiments of *TRY* and *GL3* using the three inhibition scenarios. Because the model parameters are unknown, we cannot directly test the accordance of the different simulation results with our experimental findings. However, we can confine the model parameters to biologically meaningful ranges and evaluate the accordance within these ranges (see Table III). We randomly sampled parameters inside the reduced parameter space and tested for each sample whether the following five criteria are fulfilled: (1) pattern formation from homogeneous initial conditions is possible, i.e. the parameter set is inside the Turing space; (2) *35S:TRY* overexpression leads to a loss of patterning; (3) *GL2:TRY* overexpression leads to a loss of patterning; (4) *35S:GL3* overexpression yields a higher trichome density compared to wild type; (5) *GL2:GL3* overexpression results in a similar trichome density compared to wild type. For details of the simulations, see Materials and methods.

The frequency of matched criteria for the three competition scenarios is presented on a logarithmic scale in Figure 6. The single competitive inhibition scenario meets each criterion most often, followed by the double competitive scenario. The uncompetitive scenario matches each criterion at least one order of magnitude less compared to the two other cases. In particular, the frequency of randomly hitting the Turing space is only 2%, whereas it is more than 30% in the two other scenarios. Interestingly, we found parameter samples that match all criteria simultaneously only for the single and double competitive scenarios but not for the uncompetitive case. As we could not reproduce all the experimental overexpression phenotypes simultaneously with the uncompetitive

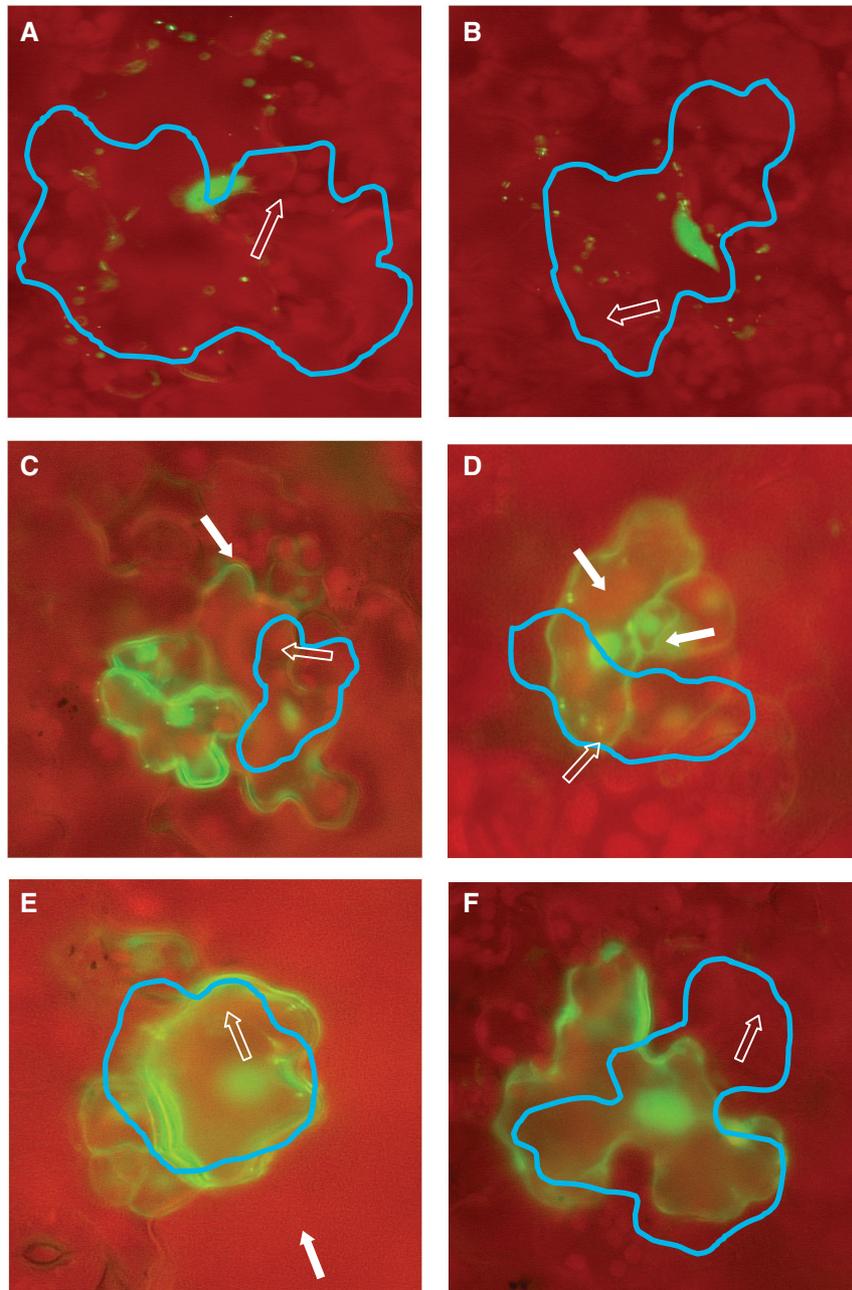


Figure 3 Intercellular mobility of proteins involved in trichome patterning. Translational fusions of GL1, GL3, TRY and CPC under the control of the 35S promoter (*35S::GFP::GL1*, *35S::GFP::GL3*, *35S::GFP::TRY* and *35S::GFP::CPC*) are co-bombarded with *35S::YFP::peroxisome* into *Arabidopsis* cotyledons and rosette leaves by the micro-projectile bombardment method and analysed after 6–10 h. Cells expressing fluorescent-labelled peroxisomes are highlighted by a blue line. One peroxisome in the initially transformed cell is indicated by an open arrow. A cell showing fluorescence in the immediate neighbourhood is marked with a white arrow. **(A)** GFP:GL1 and **(B)** GFP:GL3 fluorescence are seen only in the transformed cell. **(C)** GFP:TRY and **(D)** GFP:CPC fluorescence are found in neighbouring cells. **(E)** GFP alone is also found in neighbouring cells. **(F)** GFP:YFP is not mobile.

inhibition scenario, we conclude that it is not consistent with our data.

Single competitive inhibition is a submodel of double competitive inhibition as it contains only the GL3 TRY interaction, whereas the latter additionally contains the GL1 TRY interaction. Hence, we investigate the relation between the parameter samples matching all criteria of these two models simultaneously. In particular, we ask whether the double competitive inhibition is only able to meet all criteria in

the extreme case of single competitive inhibition. We calculate the pairwise correlations between all parameters of the double competitive inhibition model and find a strong negative correlation ($\rho_{k_3, k_7} = -0.55$, $P < 0.01$) between the binding rates of TRY to GL1 and GL3. Parameter sets with comparable binding affinities are found far less frequent than these two extreme cases (see Supplementary Figure 3). Thus, the double competitive inhibition explains in most cases all experimental data either by a strong binding affinity of TRY to GL3 and a

weak binding affinity to GL1 or vice versa. Therefore, we conclude that single competitive inhibition is sufficient to explain all experimental findings and double competitive inhibition is not necessary to describe trichome patterning in the context of our data.

Table I Protein movement in the leaf epidermis

Fusion protein	Protein size (kDa)	Cotyledons			Rosette leaves		
		Total	Movement	%	Total	Movement	%
GFP-TRY	41.5	190	65	34	111	37	33
GFP-CPC	39.9	132	49	37	188	65	34
GFP-GL1	54.9	101	0	0	68	0	0
GFP-GL2	111.7	72	0	0	62	0	0
GFP-GL3	99.1	52	0	0	57	0	0
GFP	28.55	206	54	26	100	31	31
GFP-YFP	55.1	147	0	0	103	4	3

A qualitative comparison between the simulated and experimental overexpression of *GL3* in the single competitive inhibition scenario is presented in Figure 5C–G. Note that the irregularities of the simulated trichome pattern are due to the fact that only TRY acts non-cell autonomously and can also be observed experimentally. In Figure 5H and I, the effect of the *GL3* and *TRY* overexpression is illustrated by a two-dimensional section of the parameter space. Parameter regions that

Table II Number of trichome neighbouring cell showing fluorescence

Fusion protein	% of cells surrounding the transformed one						
	1	2	3	4	5	6	7
GFP-TRY	47.5	32.5	7.5	8.75	1.25	1.25	1.25
GFP-CPC	42.37	35.59	18.64	3.39	0	0	0
GFP	31.25	16.25	16.25	8.75	8.75	8.75	10

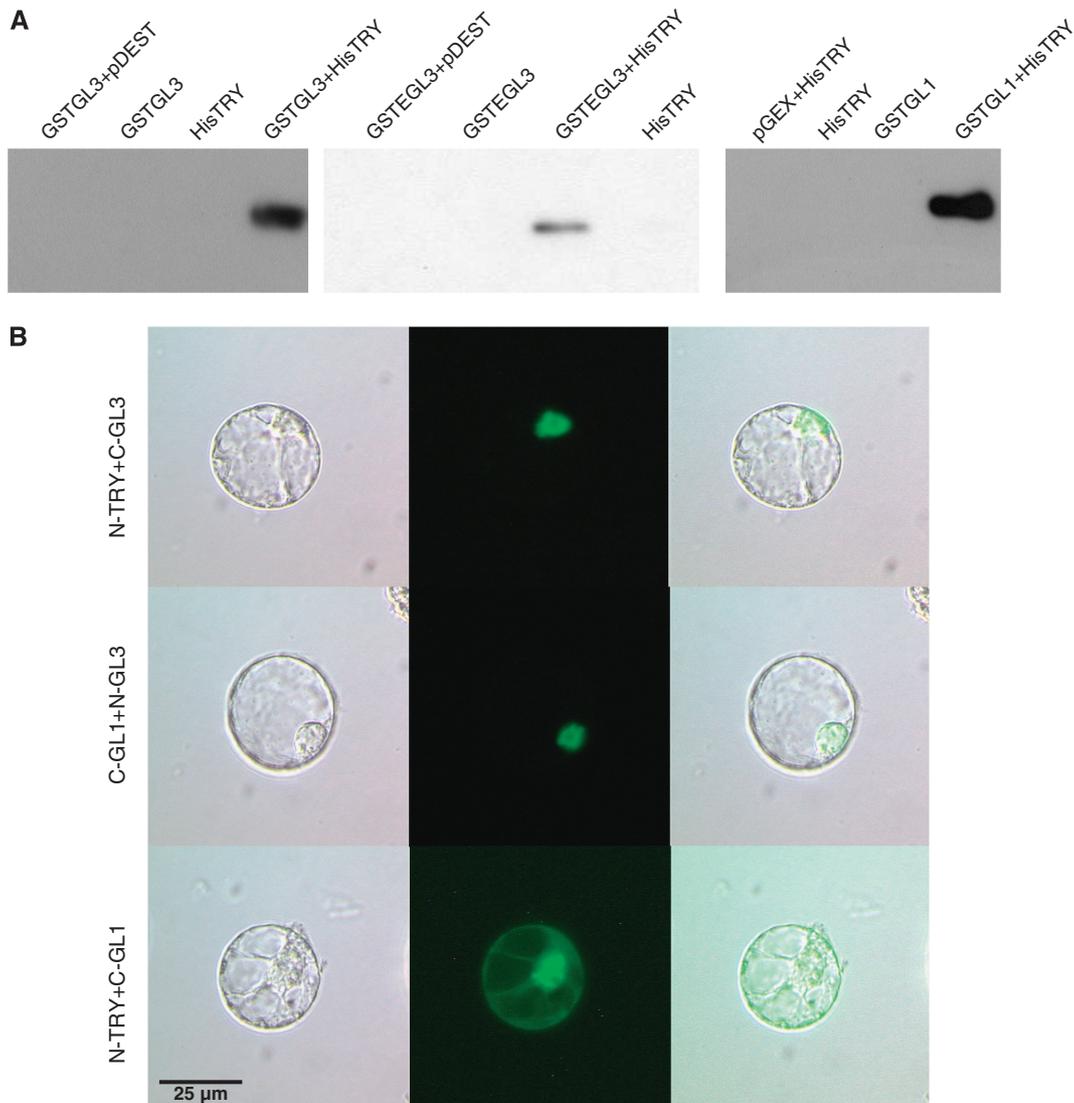


Figure 4 Molecular interactions of TRY with GL3, EGL3 and GL1. **(A)** The corresponding single protein fusions or combinations were purified by a GST pull down and detected on a western blot using an anti-His antibody. **(B)** BiFC was used to detect the interaction between TRY and GL1 or GL3 in protoplasts. Left lane shows a light micrograph, middle lane shows the BiFC fluorescence and the right micrograph shows the overlay.

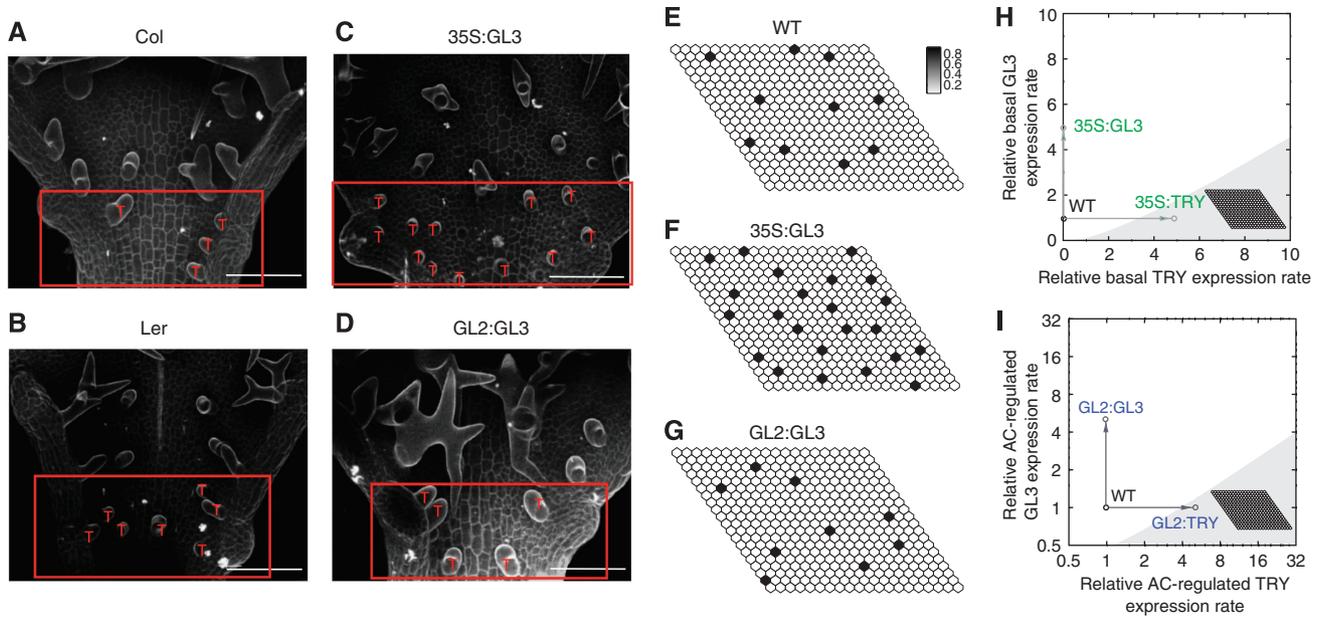


Figure 5 Results of the experimental and simulated *GL3* and *TRY* overexpressions. (**A–D**) Scanning electron microscopy. The initiation zone is highlighted by a red box and red T's denote developing trichomes. The scale bar corresponds to 50 μ m. (A) Columbia (Col) wild type. (B) Landsberg erecta (*Ler*) wild type. (C) *35S:GL3* overexpression results in a higher trichome density compared with the corresponding wild-type ecotype Columbia. (D) *GL2:GL3* overexpression results in a similar trichome density compared with the corresponding wild-type ecotype Landsberg erecta. (**E–G**) Simulation results for the single competitive inhibition scenario. The relative level of the active complex AC is given in grey scale. High level indicates a future trichome. The parameter values are given in Materials and methods. (E) Wild type (WT). (F) *35S:GL3* overexpression. (G) *GL2:GL3* overexpression. The change of the trichome density observed in the experiments is reflected in the simulations. (**H, I**) Two-dimensional sections of the parameter space. White area denotes the Turing space. The wild-type parameter set is indicated by the black circle and the corresponding simulated pattern is shown in (E). (H) Effect of *35S:GL3* and *35S:TRY* overexpression in the single competitive scenario. The overexpression is simulated by increasing the rescaled basal expression rates k_4 and k_9 of *GL3* and *TRY*, respectively. The *35S:TRY* overexpression (right arrow) leads to a loss of trichome patterning (shaded area). Conversely, a five-fold *35S:GL3* overexpression relative to wild type level (top arrow) preserves the ability to form patterns (white area). The corresponding pattern is shown in (F). (I) Effect of *GL2:GL3* and *GL2:TRY* overexpression in the single competitive scenario. The overexpression is simulated by five-fold increased AC-regulated expression rates k_5 and k_{10} of *GL3* and *TRY*, respectively. The corresponding pattern of five-fold *GL2:GL3* overexpression is shown in (G).

Table III Parameters of the mathematical model

Dimensionless parameter	Functional relation to dimensional parameters	Biologically reasonable parameter range	SCI: median (IQR) single competition scenario (median (IQR))	DCI: median (IQR) double competitive scenario (Median (IQR))
k_1	$\sigma_1\beta_1/\rho_1^2$	0.01–100	8.37 (25.71)	4.07 (11.90)
k_2	σ_1/ρ_1	0–100	4.02 (7.12)	2.47 (2.92)
k_3	β_2/β_1	0.01–100	0	0.57 (8.68)
k_4	$\sigma_2\beta_1/\rho_1^2$	0.01–100	9.49 (32.93)	13.97 (39.89)
k_5	σ_2/ρ_1	0–100	2.40 (2.98)	2.89 (3.79)
k_6	ρ_2/ρ_1	0.1–10	1.27 (3.71)	1.29 (3.61)
k_7	β_3/β_1	0.01–100	13.18 (31.54)	0.91 (12.77)
k_8	γ_1/ρ_2	0	0	0
k_9	$\sigma_3\beta_1/\rho_1^2$	0	0	0
k_{10}	α_3/β_1	0.1–1	0.46 (0.44)	0.46 (0.43)
k_{11}	ρ_3/ρ_1	0.1–10	0.83 (1.91)	1.60 (3.75)
k_{12}	β_4/β_1	0.01–100	0	0
k_{13}	γ_2/ρ_3	0.1–100	35.16 (44.28)	44.51 (47.97)
k_{14}	ρ_4/ρ_1	0.1–10	0.82 (1.20)	0.72 (0.97)

The last two columns give the median and IQR of all parameter samples that meet the overexpression criteria as given in the text. Single competitive inhibition (SCI), double competitive inhibition (DCI) and interquartile range (IQR).

give rise to a Turing instability, as determined from a linear stability analysis, are indicated in white, whereas regions outside the Turing space are given in grey. For details of the analysis, see the Supplementary information. This local visualization of the Turing space provides an explanation

why the overexpression of *GL3* and *TRY* yield different phenotypes. Because of the local convexity of the Turing space, an increased *TRY* expression yields a parameter set outside the Turing space and consequently leads to a loss of pattern. In contrast, an increased *GL3* expression preserves the

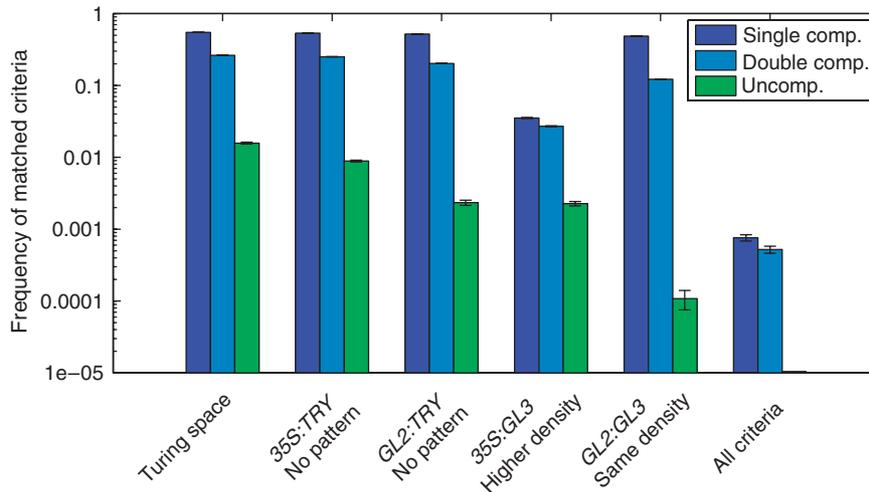


Figure 6 Frequency of matched criteria for the three inhibition scenarios. The frequency of each criterion is determined from 10^6 random samples of the parameter space. The criteria reflect the agreement between the results of a model simulation and the experimentally observed phenotype in wild type and the four overexpression situations. Note the logarithmic scale of the y axis. Although the single and double competition scenarios fulfil all criteria within the same order of magnitude, the frequency of matches for the uncompetitive scenario is one order of magnitude lower than both other cases. Only the single and the double competition scenario, respectively, can match all criteria simultaneously. Mean and standard deviation of each criterion are determined from 10 blocks of 10^5 samples. For details of the criteria, see Materials and methods.

pattern-forming ability of the model. Note that we only consider the relative increase in expression rates, as the absolute values of the expression rates in wild type and mutant are unknown. The increased sensitivity towards a manipulation of the TRY level in comparison to the GL3 level holds for constitutive as well as AC-driven overexpression. It is noteworthy that this increased sensitivity is not a local feature of the Turing space at this particular parameter set given in Figure 5, but hold for very different parameter sets as indicated by the results presented in Figure 6 and Supplementary Figure 2.

Discussion

The use of phenomenological descriptions in the study of development has a long tradition (Hofmeister, 1868; Thompson, 1942). Essential principles of development were formulated as mathematical models that describe the observed developmental pattern on a phenomenological basis (Gierer and Meinhardt, 1972; Cooke and Zeeman, 1976; Othmer, 1977; Mitchison, 1977; Erneux, 1978; Mitchison, 1980). The overwhelming advances in the molecular understanding of developmental processes in the last decades demand an adaptation of this successful approach to the details of current knowledge and experimental possibilities. Mechanistic in contrast to phenomenological descriptions can fill this gap. Mechanistic models can predict the effect of specific genetic or biochemical interventions and can suggest the design of specific experiments. In this study, we present a mechanistic model for trichome patterning that can be used to address several experimentally feasible interventions of the system.

Our study reveals several new properties of trichome patterning in *Arabidopsis* leaves. First, we show that GL1 and GL3 are actually positive regulators for the expression of TRY and CPC, which has been assumed previously. This fact is a necessary requirement of theoretical models and has not

been experimentally confirmed before. Second, we demonstrate by micro-projectile bombardment that the inhibitors TRY and CPC can move into neighbouring cells. In contrast to the root system, we find that GL3 is cell autonomous. Both results are in agreement with the requirement of the activator-inhibitor model for a farther transport of the inhibitors compared to the activators. As predicted by theoretical models including only the mobility of the inhibitor, the resulting pattern is less regular than in a model including the mobility of both substances. This is also consistent with the less orderly pattern observed in the initiation zone of the young leaf. Further, we confirm the previously shown interaction of GL3 and TRY and find an additional interaction between TRY and GL1. This opens the possibility for different ways how TRY can exert its inhibitory function. We construct three alternative models that reflect different inhibition scenarios: (1) single competitive inhibition in which TRY binds to free GL3 and blocks the formation of the active complex, (2) double competitive inhibition that additionally includes the binding of TRY to free GL1 and (3) uncompetitive inhibition whereby TRY binds only to the activator complex and renders it inactive. Analysis of the three models suggests experimental interventions in the form of different overexpressions to identify the most relevant of these scenarios. We use the 35S promoter and the promoter of the downstream target GL2 to overexpress GL3 and TRY either constitutively or under the control of the active complex, respectively. For each of the three scenarios, we compare simulation results with the overexpression phenotypes. This comparison depends on the particular choice of parameter values. As these are unknown, we employ a global sampling strategy that allows us to evaluate the different scenarios and identify constraints on the parameters. Using this approach, we can predict that the interaction between TRY and GL3 is the most relevant for trichome patterning. In particular, the uncompetitive inhibition scenario cannot reproduce our experimental findings,

whereas the double competition scenario mostly does so in the extreme case of single competition. Interestingly, the single competitive inhibition scenario tolerates larger parameter variations than both other scenarios while still forming the correct patterns (cf. Supplementary Figure 4). In this sense, the model can explain why the trichome patterning system is robust and can yield a similar qualitative output despite naturally occurring perturbations, e.g. in the form of genetic and environmental variability.

Although we have considered only few components of the patterning system, our combined experimental and theoretical effort reveals specific system properties far beyond any intuitive judgement. Yet the model is not sufficient to explain many additional observations, e.g. the single and double mutant phenotypes of the inhibitors. Additional experiments on the specific properties of the inhibitors are needed. With joint endeavour of theory and experiment, it should be possible to uncover the principles of trichome pattern formation.

Materials and methods

Mathematical model

From the interactions depicted in Figure 1, we derive the following system of coupled ordinary differential equations describing the time evolution of GL1, GL3, TRY and the active complex (AC).

$$\partial_t[\text{GL1}]_j = \sigma_1 + \alpha_1[\text{AC}]_j - [\text{GL1}]_j(\rho_1 + \beta_1[\text{GL3}]_j + \beta_2[\text{TRY}]_j) \quad (1)$$

$$\partial_t[\text{GL3}]_j = \sigma_2 + \alpha_2[\text{AC}]_j - [\text{GL3}]_j(\rho_2 + \beta_1[\text{GL1}]_j + \beta_3[\text{TRY}]_j) + \gamma_1 \langle [\text{GL3}]_j \rangle \quad (2)$$

$$\partial_t[\text{TRY}]_j = \sigma_3 + \alpha_3[\text{AC}]_j^2 - [\text{TRY}]_j(\rho_3 + \beta_2[\text{GL1}]_j + \beta_3[\text{GL3}]_j + \beta_4[\text{AC}]_j) + \gamma_2 \langle [\text{TRY}]_j \rangle \quad (3)$$

$$\partial_t[\text{AC}]_j = \beta_1[\text{GL1}]_j[\text{GL3}]_j - [\text{AC}]_j(\rho_4 + \beta_4[\text{TRY}]_j) \quad (4)$$

The model does not include an equation describing the time evolution of any inactive complex as these do not feed back into the system. Note that the square in equation (3) is needed for the stability of the system. For biological relevance, all variables and parameters have to be non-negative. The model is formulated on a hexagonal grid with coordinates $j=(y, x)$ as depicted in Supplementary Figure 1. Here, $1 \leq x \leq x_{\max}$ and $1 \leq y \leq y_{\max}$, and x_{\max} and y_{\max} are the number of cells in x and y directions, respectively. We assume periodic boundary conditions of the grid. To describe the coupling between neighbouring cells, we define the passive transport of a variable $[C]_i$ as

$$\langle [C]_{y,x} \rangle = [C]_{y-1,x} + [C]_{y+1,x} + [C]_{y,x-1} + [C]_{y,x+1} + [C]_{y+1,x-1} + [C]_{y-1,x+1} - 6[C]_{y,x} \quad (5)$$

where C stands for GL3 or TRY. The parameters in our model are rates for basal expression (σ_i), regulated expression (α_i), degradation (ρ_i), complex formation (β_i) and transport (γ_i) of the corresponding species. Note that the basal expression of TRY is only incorporated to enable simulations of 35S:TRY overexpression experiments ($\sigma_3 > 0$); in all other cases, $\sigma_3 = 0$. The complex formation rates, which together determine the type and strength of the inhibition, are adapted to reflect three different scenarios. These are single competitive ($\beta_2 = 0, \beta_3 > 0, \beta_4 = 0$), double competitive ($\beta_2 > 0, \beta_3 > 0, \beta_4 = 0$) and uncompetitive ($\beta_2 = 0, \beta_3 = 0, \beta_4 > 0$) inhibition. As all model parameters are unknown, a rescaling of time and concentration is applied. This approach allows us to reduce the total number of model parameters and to confine the resulting dimensionless parameters to biologically reasonable ranges,

while retaining a mathematically equivalent set of equations. All concentrations are rescaled by the factor β_1/ρ_1 . Time is expressed in units of half-life of GL1, i.e. $\tau = \rho_1 t$. The resulting dimensionless model has the following form:

$$\partial_\tau[\text{gl1}]_j = k_1 + k_2[\text{ac}]_j - [\text{gl1}]_j(1 + [\text{gl3}]_j + k_3[\text{try}]_j) \quad (6)$$

$$\partial_\tau[\text{gl3}]_j = k_4 + k_5[\text{ac}]_j - [\text{gl3}]_j(k_6 + [\text{gl1}]_j + k_7[\text{try}]_j) + k_6 k_8 \langle [\text{gl3}]_j \rangle \quad (7)$$

$$\partial_\tau[\text{try}]_j = k_9 + k_{10}[\text{ac}]_j^2 - [\text{try}]_j(k_{11} + k_3[\text{gl1}]_j + k_7[\text{gl3}]_j + k_{12}[\text{ac}]_j) + k_{11} k_{13} \langle [\text{try}]_j \rangle \quad (8)$$

$$\partial_\tau[\text{ac}]_j = [\text{gl1}]_j[\text{gl3}]_j - [\text{ac}]_j(k_{14} + k_{12}[\text{try}]_j) \quad (9)$$

Table III lists the dimensionless parameters together with their corresponding functional relation to the dimensional parameters. Note that due to our experimental finding that GL3 is cell autonomous, we set $k_8 = 0$ in all numerical simulations.

Numerical simulation

All simulations are performed with MATLAB from Math Works Inc. The ODE system (6)–(9) is integrated using the ode15s function of MATLAB, which is designed to solve stiff ODEs. As we could not obtain an analytical expression for the homogeneous steady state of equations (6)–(9), we determined the steady state by numerical integration of the single-cell model starting with zero initial conditions for all protein concentrations. This steady state is used with additional 1% random variation per cell as initial conditions for the simulation of the grid of cells, including spatial coupling.

Parameter scan

For each inhibition model, 10^6 random parameter samples are drawn from an exponential distribution to sample the orders of magnitude of each parameter uniformly. Each sample is confined to the ranges specified in Table III. For a given parameter sample, the condition for Turing instability is checked by a linear stability analysis as described in detail in the Supplementary information. Basal GL3 overexpression is simulated by a five-fold increase in the expression rate k_4 . As a basal expression of TRY is absent in *planta*, 35S:TRY overexpression is simulated by setting the basal expression rate of TRY, i.e. k_9 , equal to the value of k_4 in the simulated 35S:GL3 overexpression. The overexpression of GL3 and TRY under the GL2 promoter is simulated by a five-fold increased rate of active complex-dependent expression, i.e. rate k_5 and k_{10} , respectively, as the active complex binds to the promoter of GL2. The effect of each of these four parameter perturbations is checked by a linear stability analysis (for details of the analysis, see Supplementary information). Additionally, numerical simulation of the 35S:GL2 and GL2:GL3 plants is used to determine the trichome density of the corresponding plants. The simulated 35S:GL3 plant is said to fulfil the experimental observation of an increased trichome density if it is at least 1.5 times higher than the simulated WT density. The density of the simulated GL2:GL3 plants $D_{\text{GL2:GL3}}$ is said to match the WT density D_{WT} if $(D_{\text{GL2:GL3}} - D_{\text{WT}})^2 \leq 0.0004$ holds.

Parameters used for simulation presented in Figure 5

Wild-type parameter values: $k_1 = 8.2707$, $k_2 = 3.4869$, $k_3 = 0$, $k_4 = 15.0952$, $k_5 = 1.3488$, $k_6 = 0.4503$, $k_7 = 7.9509$, $k_8 = 0$, $k_9 = 0$, $k_{10} = 0.4117$, $k_{11} = 0.9565$, $k_{12} = 0$, $k_{13} = 10$ and $k_{14} = 0.2703$. Parameter values of the overexpressed mutants are chosen as described above.

Plant material, growth condition and genetic methods

Plants were grown at 22°C for 16 h white light a day. The *Arabidopsis* lines TRY:GUS, gl1-1, gl3, gl3 egl3, 35S:TRY and 35S:CPC have been described previously (Oppenheimer et al, 1991; Larkin et al, 1993;

Hulskamp *et al*, 1994; Lloyd *et al*, 1994; Wada *et al*, 1997b; Szymanski and Marks, 1998; Walker *et al*, 1999b; Schellmann *et al*, 2002). Crosses of the *TRY:GUS* lines to recessive mutants were performed by using the respective GUS line as male parent. The F2 generation was screened for BASTA resistance.

For the swapping experiment, *GL2:GL3* lines have been described previously (Kirik *et al*, 2005). *35S:GL3* was generated by recombination of full-length *GL3* cDNA into pAMPAT vector. *35S:TRY* and *GL2:TRY* were generated by cloning of *TRY* cDNA in pCAMBIA 1300 (Mathur *et al*, 2003). The constructs were transformed into the *Agrobacterium* strain *GV3101* by electroporation (Bio-Rad gene pulser) and Landsberg erecta plants were transformed using the floral dip method (Clough and Bent, 1998). Transformants were selected in the T1 generation using MS plates containing 50 mg/l kanamycin or on soil with a 0.1% BASTA solution.

Constructs, biolistic transformation and BiFC

The constructs used for the transient assay in leaf epidermis were created by fusing GFP (Clontech) to the N terminus of the coding sequence of *GL1*, *GL3*, *TRY* and *CPC* and placed under the control of the *CaMV 35S* promoter. Details are available on request. Transient expression analysis was carried out by using the particle bombardment method as described previously (Mathur *et al*, 2003).

TRY, *GL1* and *GL3* were recombined into BiFC vectors (pBatTL) and transfected in *Arabidopsis* protoplast (Uhrig *et al*, 2007). The transfected cells were incubated at 23°C for 16–20 h in the dark before microscopic observation.

Histology and microscopy

GUS staining was performed as described by Malamy and Benfey (1997). Plant specimens were analysed using the LEICA-DMRE microscope equipped with a high-resolution KY-F70 3-CCD JVC camera and frame-grabbing software (DISKUS; Technisches Büro, Königswinter). Photos were edited with Adobe Photoshop 6.

Expression and purification of recombinant fusion proteins

GL1, *GL3*, *EGL3* and *TRY* cDNA were recombined into pGEX2TMGW and pDEST 17 vectors by Gateway Cloning (Invitrogen) to create GST and His fusion proteins, respectively. Recombinant proteins were expressed in *Escherichia coli* BL21DE3RIL cells (Stratagene) by the induction of GST fusion proteins with a final IPTG concentration of 0.1 mM at 37°C for 4 h and of His fusion proteins with a final concentration of IPTG of 1 mM at 37°C for 3 h. Bacteria expressing GST fusion proteins were lysed as described by Frangioni and Neel (1993) and proteins were purified through the glutathione sepharose (GE Healthcare cat. no: 17-5279-01) by batch method as described by Sambrook and Russell (2001). The buffer of the purified proteins was changed against 50 mM Tris-HCl pH 7.8, 1 mM EDTA, 150 mM NaCl, 0.1% Nonidet P-40 and 4% BSA by the Amicon Ultra 10k. Bacteria expressing His fusion proteins were pelleted after induction, and lysis was achieved by sonicating five times using 10-s pulses in the lysis buffer (100 mM NaCl, 50 mM Tris pH 7.9, 2 mM EDTA, 1% Triton X-100). His fusion proteins were purified through Ni-NTA resin (Qiagen), according to the product instructions. Final elutions were done with phosphate-buffered saline buffer containing a final concentration of 20 mM EDTA. Purified proteins were dialysed against 50 mM Tris-HCl pH 7.8, 1 mM EDTA, 150 mM NaCl. All of the buffers used contained Roche Complete Protease Inhibitor Cocktail™.

Pull down

GST and His fusion purified proteins (0.5 µg) were incubated together for 2 h at 4°C on a rocking platform. Then 50 µl of glutathione resin (Mathur *et al*, 2003; GE Healthcare cat. no: 17-5279-01) was added and the mixture was incubated further for 2 h at 4°C on a rocking platform. After incubation, the mixture was washed for five times with buffer (50 mM Tris-HCl pH 7.8, 1 mM EDTA, 150 mM NaCl, 0.1% Nonidet P-40). Pull-down assays and the mixture was washed either in the

presence or absence of BSA. SDS gel extraction buffer was added to the samples. Samples were run on SDS-PAGE and blotted against PVDF membranes. Anti-His antibodies were used for the detection of the His-tagged pulled down proteins.

Supplementary information

Supplementary information is available at the *Molecular Systems Biology* website (www.nature.com/msb).

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